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Neural Networks CMPT 419/726 Mo Chen SFU Computing Science Jan. 29, 2020

Bishop PRML Ch. 5

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#### **Neural Networks**

- Neural networks arise from attempts to model human/animal brains
  - · Many models, many claims of biological plausibility
- · We will focus on multi-layer perceptrons
  - · Mathematical properties rather than plausibility



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#### **Applications of Neural Networks**

- Many success stories for neural networks, old and new
  - Credit card fraud detection
  - Hand-written digit recognition
  - Face detection
  - Autonomous driving (CMU ALVINN)
  - Object recognition
  - Speech recognition

Network Training

Error Backpropagation

Deep Learning



Feed-forward Networks

**Network Training** 

**Error Backpropagation** 

**Deep Learning** 

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Network Training

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Feed-forward Networks

**Network Training** 

**Error Backpropagation** 

Deep Learning

#### Feed-forward Networks

• We have looked at generalized linear models of the form:

$$y(\boldsymbol{x}, \boldsymbol{w}) = f\left(\sum_{j=1}^{M} w_j \phi_j(\boldsymbol{x})\right)$$

for fixed non-linear basis functions  $\phi(\cdot)$ 

- We now extend this model by allowing adaptive basis functions, and learning their parameters
- In feed-forward networks (a.k.a. multi-layer perceptrons) we let each basis function be another non-linear function of linear combination of the inputs:

$$\phi_j(x) = f\left(\sum_{j=1}^M \cdots\right)$$

#### Feed-forward Networks

Starting with input x = (x<sub>1</sub>,...,x<sub>D</sub>), construct linear combinations:

$$a_j = \sum_{i=1}^{D} \left( w_{ji}^{(1)} x_i + x_{j0}^{(1)} \right)$$

These  $a_i$  are known as activations

- Pass through an activation function  $h(\cdot)$  to get output  $z_j = h(a_j)$ 
  - Model of an individual neuron



#### Activation Functions

- Can use a variety of activation functions
  - Sigmoidal (S-shaped)
    - Logistic sigmoid  $1/(1 + \exp(-a))$  (useful forbinary classification)
    - Hyperbolic tangent  $tanh(\cdot)$
  - Radial basis function  $z_j = \sum_i (x_i w_{ji})^2$  Softmax
  - - Useful for multi-class classification
  - Identity •
    - Useful for regression
  - Threshold
  - ٠ ...
- Needs to be differentiable for gradient-based learning (later)
- Can use different activation functions in each unit •



#### **Activation Functions**

#### Common choices of activation functions Softplus: $log(1 + e^x)$

Hyperbolic tangent: tanh x

# Rectified linear unit (ReLU): max(0, x)

Key feature: easy to differentiate



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#### Feed-forward Networks



- Connect together a number of these units into a feedforward network (DAG)
- · Above shows a network with one layer of hidden units
- Implements function

$$y_k(x,w) = h^{(2)} \left( \sum_{j=1}^M w_{kj}^{(2)} h^{(1)} \left( \sum_{i=1}^D w_{ij}^{(1)} x_i + w_{j0}^{(1)} \right) + w_{k0}^{(2)} \right)$$

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## **Network Training**

- Given a specified network structure, how do we set its parameters (weights)?
  - As usual, we define a criterion to measure how well our network performs, optimize against it
- For regression, training data are  $(x_n, t_n), t_n \in \mathbb{R}$ 
  - Squared error naturally arises:

$$E(w) = \sum_{n=1}^{N} \{y(x_n, w) - t_n\}^2$$

 For binary classification, this is another discriminative model, ML:

$$p(t|w) = \prod_{n=1}^{N} y_n^{t_n} \{1 - y_n\}^{1 - t_n}$$
$$E(w) = -\sum_{n=1}^{N} \{t_n \ln(y_n) + (1 - t_n) \ln(1 - y_n)\}$$

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#### **Parameter Optimization**



- For either of these problems, the error function *E*(*w*) is nasty
  - Nasty = non-convex
  - Non-convex = has local minima

#### A Non-Convex function



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#### Aside: Optimization Program

 $\begin{array}{ll} \text{minimize} & f(x) \\ \text{subject to} & g_i(x) \leq 0, i = 1, \dots, n \\ & h_j(x) = 0, j = 1, \dots, m \end{array}$ 



- Very difficult to solve in general
  - Trade-offs to consider: computation time, solution optimality
- Easy cases:
  - Find global optimum for linear program: f, g<sub>i</sub>, h<sub>i</sub> are linear
  - Find global optimum for **convex program**: f,  $g_i$  are convex,  $h_j$  is linear
  - Find local optimum for **nonlinear program**: f,  $g_i$ ,  $h_j$  are differentiable
- Neural Networks: Nonlinear and unconstrained

#### **Convex Functions**



#### Convex function

 $f(\theta x + (1 - \theta)y) \le \theta f(x) + (1 - \theta)f(y) \text{ for all } x, y \in \mathbb{R}^n, \text{ for all } \theta \in [0, 1]$ 

- Sublevel sets of convex functions,  $\{x: f(x) \le C\}$ , are convex
  - Convex shape C:  $x_1, x_2 \in C, \theta \in [0,1] \Rightarrow \theta x_1 + (1 - \theta) x_2 \in C$



#### **Convex Functions**

Convex function

 $\begin{aligned} f(\theta x + (1 - \theta)y) &\leq \theta f(x) + (1 - \theta)f(y) \text{ for all } x, y \\ &\in \mathbb{R}^n, \text{ for all } \theta \in [0, 1] \end{aligned}$ 



- Sublevel sets of convex functions,  $\{x: f(x) \le C\}$ , are convex
  - Convex shape C:
    - $x_1, x_2 \in \mathcal{C}, \theta \in [0,1] \Rightarrow \theta x_1 + (1-\theta)x_2 \in \mathcal{C}$
  - Superlevel sets of convex functions are not convex!



#### Common Convex Functions on ${\mathbb R}$

- $f(x) = e^{ax}$  is convex for all  $x, a \in \mathbb{R}$
- $f(x) = x^a$  is convex on x > 0 if  $a \ge 1$  or  $a \le 0$ ; concave if 0 < a < 1
- $f(x) = \log x$  is concave
- $f(x) = x \log x$  is convex for x > 0 (or  $x \ge 0$  if defined to be 0 when x = 0)



#### Common Convex Functions on $\mathbb{R}^n$



- Every norm on  $\mathbb{R}^n$  is convex
- $f(x) = \max(x_1, x_2, \dots, x_n)$  is convex

• 
$$f(x) = \frac{x_1^2}{x_2}$$
 (for  $x_2 > 0$ )

- Log-sum-exp softmax:  $f(x) = \frac{1}{k} \log(e^{kx_1} + e^{kx_2} + \dots + e^{kx_n})$
- Geometric mean:  $f(x) = (\prod_{i=1}^{n} x_i)^{\frac{1}{n}}, x_i > 0$





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 $f(x_1, x_2) = \max(x_1, x_2)$ 

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#### **Descent Methods**

 The typical strategy for optimization problems of this sort is a descent method:

$$\boldsymbol{w}^{(\tau+1)} = \boldsymbol{w}^{(\tau)} + \Delta \boldsymbol{w}^{(\tau)}$$

- · As we've seen before, these come in many flavours
  - Gradient descent  $\nabla E(w^{(\tau)})$
  - Stochastic gradient descent  $\nabla E_n(w^{(\tau)})$
  - Newton-Raphson (second order)
- All of these can be used here, stochastic gradient descent is particularly effective
  - · Redundancy in training data, escaping local minima

#### Numerical Solution: Gradient Methods

- Start from  $x^0$  and construct a sequence  $x^k$  such that  $x^k \rightarrow x^*$ 
  - Calculate  $x^{k+1}$  from  $x^k$  by "going down the gradient"
  - Unconstrained case:  $x^{k+1} = x^k \alpha^k \nabla f(x), \ \alpha^k > 0$





#### Numerical Solution: Gradient Methods

- Start from  $x^0$  and construct a sequence  $x^k$  such that  $x^k \rightarrow x^*$ 
  - Calculate  $x^{k+1}$  from  $x^k$  by "going down the gradient"
  - Unconstrained case:  $x^{k+1} = x^k \alpha^k \nabla f(x), \ \alpha^k > 0$
- More generally,  $x^{k+1} = x^k + a^k d^k$  for some d such that

$$\nabla f(x^k) \cdot d^k < 0$$

• Tuning parameters: descent direction  $d^k$ , and step size  $\alpha^k$ 



#### **Descent Direction**

- Steepest descent:  $d^k = -\nabla f(x^k)$ 
  - $x^{k+1} = x^k \alpha^k \nabla f(x)$
  - · Simple but sometimes leads to slow convergence
- Newton's method:  $d^k = \left(\nabla^2 f(x^k)\right)^{-1} \nabla f(x^k)$ 
  - Minimize the quadratic approximation:

$$f^{k}(x) = f(x^{k}) + \nabla f(x^{k})^{\mathsf{T}}(x - x^{k}) + \frac{1}{2}(x - x^{k})^{\mathsf{T}} \mathrm{H}f(x^{k})(x - x^{k})$$

· Set gradient to zero to obtain next iterate

$$\nabla f^{k}(x) = \nabla f(x^{k}) + \mathrm{H}f(x^{k})(x - x^{k}) = 0$$
  
$$\Rightarrow x^{k+1} = x^{k} - \left(\mathrm{H}f(x^{k})\right)^{-1} \nabla f(x^{k})$$

- · Fast convergence, but matrix inverse required
- · Alternatively, use an algorithm to minimize a quadratic function



#### Step Size

• Recall 
$$x^{k+1} = x^k + \alpha^k d^k$$
, with  $\nabla f(x^k)^\top d^k < 0$ 

- Line search: choose  $\alpha^k = \min_{\alpha \ge 0} f(x^k + \alpha^k d^k)$ 
  - Requires minimization
- Constant step size:  $\alpha^k = \alpha$ 
  - May not converge
- Diminishing step size:  $\alpha^k \rightarrow 0$ 
  - Still need to explore all regions  $\sum \alpha^k = \infty$

• For example: 
$$\alpha^k = \frac{\alpha^0}{k}$$



#### Numerical Solution: Second Order Methods

minimize 
$$f(x)$$
  $\longrightarrow$  minimize  $(r^k)^{\top} d_x + \frac{1}{2} d_x^{\top} B_k d_x$   
where  $d_x \coloneqq x - x^k$ ,

• Quadratize f(x):

$$r^{k} = \nabla f(x_{k})$$
$$B_{k} = \mathrm{H}f(x_{k})$$

· Convexify if needed, eg. by removing negative eigenvalues





#### Example



#### **Computing Gradients**

- The function  $y(x_n, w)$  implemented by a network is complicated
  - It isn't obvious how to compute error function derivatives with respect to weights
- Numerical method for calculating error derivatives, use finite differences:

$$\frac{\partial E_n}{\partial w_{ji}} \approx \frac{E_n(w_{ji} + \epsilon) - E_n(w_{ji} - \epsilon)}{2\epsilon}$$

- How much computation would this take with *W* weights in the network?
  - O(|W|) per partial derivative (evaluation of  $E_n$ )
  - $O(|W|^2)$  total per gradient descent step (there are |W| partial derivatives)

Network Training

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Deep Learning



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Deep Learning

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#### Feed-forward Networks



- Connect together a number of these units into a feed-forward network (DAG)
- Above shows a network with one layer of hidden units Implements function:

$$y_{(n),k}(x_n, w) = h^{(2)} \left( \sum_{j=1}^{M} w_{kj}^{(2)} h^{(1)} \left( \sum_{l=1}^{D} w_{jl}^{(1)} x_{(n),l} + w_{j0}^{(1)} \right) + w_{k0}^{(2)} \right)$$

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#### Error Backpropagation

- Backprop is an efficient method for computing error derivatives  $\frac{\partial E_n}{\partial w_{ii}^{(m)}}$
- O(W) to compute derivatives wrt all weights
  First, feed training example x<sub>n</sub> forward through the network, storing all activations  $a_i$
- Calculating derivatives for weights connected to output nodes is easy

• e.g. For linear output nodes 
$$y_k = \sum_i w_{ki}^{(L)} z_{(n),i}^{(L-1)}$$
:  
 $\frac{\partial E_n}{\partial w_{ki}^{(L)}} = \frac{\partial}{\partial w_{ki}^{(L)}} \frac{1}{2} (y_{(n),k} - t_{(n),k})^2 = (y_{(n),k} - t_{(n),k}) z_{(n),i}^{(L-1)}$ 

 For hidden layers, propagate error backwards from the output nodes

# Opportunity to participate in robotics research

The SFU Rosie and MARS Labs are running an experiment to better understand human navigational intent – that is, predicting where a human may move to in the next several seconds.

\*Experiment takes 30 Min. \*Each participant will receive a \$10 Starbucks gift card. \*Spaces are limited to the first 40 students.

> For more information: http://tiny.cc/kdbjjz





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 $y_{(n),k}, E_n$ :

 $w_{ji}^{(m)}$ :

m: layer



$$\frac{\partial E_n}{\partial w_{ki}^{(L)}} = \frac{\partial}{\partial w_{ki}^{(L)}} \frac{1}{2} \sum_{k'} (y_{(n),k'} - t_{(n),k'})^2 = (y_{(n),k} - t_{(n),k}) z_{(n),i}^{(L-1)}$$
(\*)

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#### **Chain Rule for Partial Derivatives**

- A "reminder"
- For f(x, y), with f differentiable wrt x and y, and x and y differentiable wrt u:

$$\frac{\partial f}{\partial u} = \frac{\partial f}{\partial x}\frac{\partial x}{\partial u} + \frac{\partial f}{\partial y}\frac{\partial y}{\partial u}$$



where ∑<sub>k</sub>(…) runs over all other nodes k in the same layer (m)
Since a<sup>(m)</sup><sub>(n),k</sub> does not depend on w<sup>(m)</sup><sub>ji</sub>, all terms in the summation go to 0:

$$\frac{\partial E_n}{\partial w_{ji}^{(m)}} = \frac{\partial E_n}{\partial a_{(n),j}^{(m)}} \frac{\partial a_{(n),j}^{(m)}}{\partial w_{ji}^{(m)}}$$

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#### Error Backpropagation cont.







#### Error Backpropagation cont.

• Error  $\delta_{(n),j}^{(m)}$  can also be computed using chain rule:

$$\delta_{(n),j}^{(m)} \coloneqq \frac{\partial E_n}{\partial a_{(n),j}^{(m)}} = \sum_k \frac{\partial E_n}{\underbrace{\partial a_{(n),k}^{(m+1)}}} \frac{\partial a_{(n),k}^{(m+1)}}{\partial a_{(n),j}^{(m)}}$$

where  $\sum_{k} (\dots)$  runs over all nodes k in the layer **after**.

Eventually:

$$\delta_{(n),j}^{(m)} = (h^{(m)})' (a_{(n),j}^{(m)}) \sum_{k} \delta_{(n),k}^{(m+1)} w_{kj}^{(m+1)}$$

· A weighted sum of the later error "caused" by this weight

#### Error Backpropagation cont.

#### Eventually:

~ -

$$\begin{split} \delta_{(n),j}^{(m)} &= \left(h^{(m)}\right)' \left(a_{(n),j}^{(m)}\right) \sum_{k} \delta_{(n),k}^{(m+1)} w_{jk}^{(m+1)} \\ \text{where } \sum_{k} (\cdots) \text{ runs over all nodes } k \text{ in the layer after.} \end{split}$$

- Above recursion relation needs last set of errors:  $\delta_i^{(L)}$ 

$$\frac{\partial E_n}{\partial w_{ji}^{(m)}} = \delta_{(n),j}^{(m)} z_i^{(m-1)} \tag{by definition}$$

$$\frac{\partial E_n}{\partial w_{ji}^{(L)}} = \delta_{(n),j}^{(L)} z_{(n),i}^{(L-1)} = (y_{(n),j} - t_{(n),j}) z_{(n),i}^{(L-1)}$$
(from before (\*))

$$\delta_{(n),j}^{(L)} = y_{(n),j} - t_{(n),j}$$
 (by comparison)

#### Summary

Output Definition / forward propagation

$$y_{(n),k}(x_n, w) = h^{(m+1)} \left( \sum_{j=1}^{M} w_{jk}^{(m+1)} h^{(m)} \left( \sum_{l=1}^{D} w_{ij}^{(m)} z_{(n),l}^{(m-1)} + w_{0j}^{(m)} \right) + w_{k0}^{(m+1)} \right)$$
  
Save  $z, a$  hidden units

Save z, a

Gradient computation / backpropagation

• Last layer: 
$$\frac{\partial E_n}{\partial w_{ik}^{(L)}} = (y_{(n),k} - t_{(n),k}) z_{(n),i}^{(L-1)}$$

Previous layers: Define  $\delta_{(n),j}^{(m)} \coloneqq \frac{\partial E_n}{\partial a_{(n),j}^{(m)}}$ 

Starting from last layer,

$$\delta_{(n),j}^{(L)} = y_{(n),j} - t_{(n),j}$$

Recursion:  $\frac{\partial E_n}{\partial w_{ij}^{(m)}} = \delta_{(n),j}^{(m)} z_{(n),i}^{(m-1)}$ ,



 $x_0$ 



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O(W)

U(W)

#### Summary

Output Definition / forward propagation

$$y_{(n),k}(x_n, w) = h^{(m+1)} \left( \sum_{j=1}^{M} w_{jk}^{(m+1)} h^{(m)} \left( \sum_{i=1}^{D} w_{ij}^{(m)} z_{(n),i}^{(m-1)} + w_{0j}^{(m)} \right) + w_{k0}^{(m+1)} \right)$$

• Save *z*, *a* 



where 
$$\delta_{(n),j}^{(m)} = (h^{(m)})' (a_{(n),j}^{(m)}) \sum_{k} \delta_{k}^{(m+1)} w_{jk}^{(m+1)}$$

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#### **Descent Methods**

#### Error function:

$$E(w) = \frac{1}{2} \sum_{n=1}^{N} \sum_{k} (y_{(n),k} - t_{(n),k})^{2}, \quad E_{n}(w) = \frac{1}{2} \sum_{k} (y_{(n),k} - t_{(n),k})^{2}$$

- y(x, w) is a neural network, very complex
- Cannot solve  $\arg \min E(w)$  explicitly (like in linear
- regression)Gradient Descent:

$$\boldsymbol{w}^{(\tau+1)} = \boldsymbol{w}^{(\tau)} - \eta^{(\tau)} \nabla E(\boldsymbol{w}^{(\tau)})$$

- Stochastic Gradient Descent:
  - n chosen randomly

$$\boldsymbol{w}^{(\tau+1)} = \boldsymbol{w}^{(\tau)} - \eta^{(\tau)} \nabla E_n(\boldsymbol{w}^{(\tau)})$$

• A batch  $\mathcal{N}$  chosen randomly

$$\boldsymbol{w}^{(\tau+1)} = \boldsymbol{w}^{(\tau)} - \eta^{(\tau)} \sum_{n \in \mathcal{N}} \nabla E_n (\boldsymbol{w}^{(\tau)})$$

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#### **Tensorflow Playground**

<u>https://playground.tensorflow.org</u>

Network Training

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- Collection of important techniques to improve performance:
  - Multi-layer networks
  - Convolutional networks, parameter tying
  - Hinge activation functions (ReLU) for steeper gradients
  - Momentum
  - Drop-out regularization
  - Sparsity
  - Auto-encoders for unsupervised feature learning
  - ...
- Scalability is key, can use lots of data since stochastic gradient descent is memory-efficient, can be parallelized

#### Hand-written Digit Recognition

- MNIST standard dataset for hand-written digit recognition
  - 60000 training, 10000 test images

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#### LeNet-5, circa 1998



- · LeNet developed by Yann LeCun et al.
  - Convolutional neural network
    - Local receptive fields (5x5 connectivity)
    - Subsampling (2x2)
    - Shared weights (reuse same 5x5 "filter")
    - Breaking symmetry

Network Training

Deep Learning

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#### ImageNet



- ImageNet standard dataset for object recognition in images (Russakovsky et al.)
  - 1000 image categories, ≈1.2 million training images (ILSVRC 2013)

Vetwork Training

Deep Learning

#### GoogLeNet, circa 2014



- GoogLeNet developed by Szegedy et al., CVPR 2015
- Modern deep network
- ImageNet top-5 error rate of 6.67% (later versions even better)
- Comparable to human performance (especially for fine-grained categories)

Network Training

Error Backpropagation

Deep Learning

#### ResNet, circa 2015



- ResNet developed by He et al., ICCV 2015
- 152 layers
- ImageNet top-5 error rate of 3.57%
- Better than human performance (especially for fine-grained categories)

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#### Key Component 1: Convolutional Filters

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- Share parameters across network
- Reduce total number of parameters
- Provide translation invariance, useful for visual recognition

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# **Common Operations**

- Fully connected (dot product)
- Convolution
  - Translationally invariant
  - Controls overfitting
- Pooling (fixed function)
  - Down-sampling
  - Controls overfitting
- Nonlinearity layer (fixed function)
  - Activation functions, e.g. ReLU



#### Example: Small VGG Net From Stanford CS231n



# Neural Network Architectures

- Convolutional neural network (CNN)
  - · Has translational invariance properties from convolution
  - Common used for computer vision
- Recurrent neural network RNN
  - Has feedback loops to capture temporal or sequential information
  - Useful for handwriting recognition, speech recognition, reinforcement learning
  - Long short-term memory (LSTM): special type of RNN with advantages in numerical properties
- Others
  - General feedforward networks, variational autoencoders (VAEs), conditional VAEs, generative adversarial networks





# Training Neural Networks

- Data preprocessing
  - Removing bad data
  - Transform input data (e.g. rotating, stretching, adding noise)
- Training process (optimization algorithm)
  - Choice of loss function (eg. L1 and L2 regularization)
  - Dropout: randomly set neurons to zero in each training iteration
  - Learning rate (step size) and other hyperparameter tuning
- Software packages: efficient gradient computation
  - Caffe, Torch, Theano, TensorFlow

#### Key Component 2: Rectified Linear Units (ReLUs)



- Vanishing gradient problem
  - If derivatives very small, no/little progress via stochastic gradient descent
  - Occurs with sigmoid function when activation is large in absolute value

ReLU: 
$$h(a_j) = \max(0, a_j)$$

- Non-saturating, linear gradients (as long as non-negative activation on some training data)
- Sparsity inducing

#### Key Component 3: Many, Many Layers



- **ResNet**: ≈152 layers ("shortcut connections")
- GoogLeNet: ≈27 layers ("Inception" modules)
- VGG Net: 16-19 layers (Simonyan and Zisserman, 2014)
- AlexNet: 8 layers (Krizhevsky et al., 2012)

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#### Key Component 3: Many, Many Layers



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#### Key Component 4: Momentum

- Trick to escape plateaus / local minima
- Take exponential average of previous gradients

$$\frac{\overline{\partial E_n}^{\tau}}{\partial w_{ji}}^{\tau} = \frac{\overline{\partial E_n}^{\tau}}{\partial w_{ji}}^{\tau} + \alpha \frac{\overline{\partial E_n}^{\tau-1}}{\partial w_{ji}}$$

· Maintains progress in previous direction

## Key Component 5: Asynchronous Stochastic Gradient Descent



- Big models won't fit in memory
- Want to use compute clusters (e.g. 1000s of machines) to run stochastic gradient descent
- How to parallelize computation?
- Ignore synchronization across machines
  - Just let each machine compute its own gradients and pass to a server storing current parameters
  - Ignore the fact that these updates are inconsistent
  - Seems to just work (e.g. Dean et al. NIPS 2012)

#### Key Component 6: Learning Rate Schedule



• How to set learning rate  $\eta$ ?:

$$\boldsymbol{w}^{\tau} = \boldsymbol{w}^{\tau-1} + \eta \nabla \boldsymbol{w}$$

- Option 1: Run until validation error plateaus. Drop learning rate by x%
- Option 2: Adagrad, adaptive gradient. Per-element learning rate set based on local geometry (Duchi et al. 2010)

#### Key Component 7: Data Augmentation



- Augment data with additional synthetic variants (10x amount of data)
- Or just use synthetic data, e.g. Sintel animated movie (Butler et al. 2012)

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#### Key Component 8: Data and Compute



- · Get lots of data (e.g. ImageNet)
- Get lots of compute (e.g. CPU cluster, GPUs)
- Cross-validate like crazy, train models for 2-3 weeks on a GPU
- Researcher gradient descent (RGD) or Graduate student descent (GSD): get 100s of researchers to each do this, trying different network structures

Error Backpropagation

Deep Learning



#### Interpretability:





#### Data efficiency:

- ImageNet: 14 million images, 20000 categories
- AlphaStar: 200 years of gameplay







- Problem formulation (what are you trying to predict?)
- Choice of model and optimization algorithm
- Data collection, post-processing
- Feature selection
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#### More information

- <u>https://sites.google.com/site/</u> <u>deeplearningsummerschool</u>
- <u>http://tutorial.caffe.berkeleyvision.org/</u>
- ufldl.stanford.edu/eccv10-tutorial
- http://www.image-net.org/challenges/LSVRC/ 2012/supervision.pdf
- Courses: Deep Learning, Natural Language Processing, Computer Vision
- Project ideas
  - · Long short-term memory (LSTM) models for temporal data
  - Learning embeddings (word2vec, FaceNet)
  - Structured output (multiple outputs from a network)
  - Zero-shot learning (learning to recognize new concepts without training data)
  - Transfer learning (use data from one domain/task, adapt to another)

#### Conclusion

- Readings: Ch. 5.1, 5.2, 5.3
- Feed-forward networks can be used for regression or classification
  - Similar to linear models, except with adaptive non-linear basis functions
  - These allow us to do more than e.g. linear decision boundaries
- Different error functions
- · Learning is more difficult, error function not convex
  - Use stochastic gradient descent, obtain (good?) local minimum
- Backpropagation for efficient gradient computation