

CMPT307: Elementary Data Structures

Week 1-3

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Outline

- ▷ linked lists
- ▷ stacks
- ▷ queues

Dictionary Operations

- ▷ a dictionary has data items a_i , indexed by **key** i for $i \in \mathbb{N}$
- ▷ assume key values are unique

Basic dictionary operations

- ▷ printing data w.r.t. sorted keys
 - ▷ search
 - ▷ insertion
 - ▷ deletion
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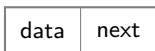
Lists

arrays

- ▷ advantages: simple and fast
- ▷ disadvantages
 - * must specify size n at construction
 - * n is often unknown and dynamic

linked list: each **node** contains

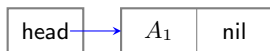
- ▷ the data item
- ▷ a pointer to the next node



```
struct node {  
    int key;  
    int val;  
    struct node *next;  
};
```

Linked Lists

list L with a **head**: initially **nil**

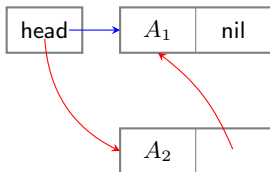


insert the first node

- ▷ set **next** to nil
- ▷ set **head** to point to the new node

Insertion

insert the second node



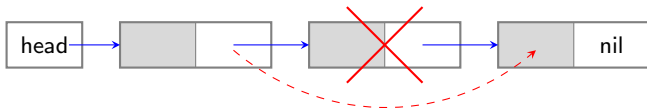
$LIST-INSERT(L, x)$

- 1 **if** $L.head \neq nil$ **then**
 - 2 $x.next = L.head$;
 - 3 $L.head = x$;
-

can we add x to the tail?

Deletion

remove an element x from L



LIST-DELETE(L, x)

```
1 prev = L.head;
2 if prev == x then
3   | L.head = x.next ;           // x is the head of L
4 else
5   | while prev.next ≠ x do
6     | prev = prev.next;
7   | prev.next = x.next;
```

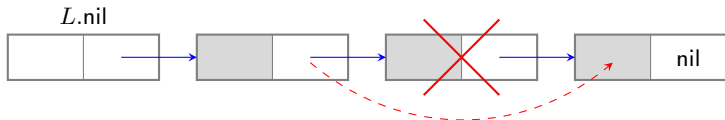
find the first element with **key** k in list L

$LIST_SEARCH(L, k)$

```
1  $x = L.head;$   
2 while  $x \neq nil$  and  $x.key \neq k$  do  
3    $x = x.next;$   
4 return  $x;$ 
```

Sentinels

- ▷ a **sentinel** is a dummy object, say `L.nil`
- ▷ it allows us to simplify boundary conditions



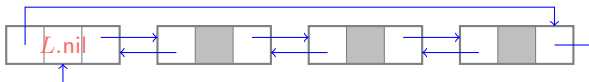
`LIST-DELETE(L,x)`

- 1 `prev = L.nil ;`
 - 2 **while** `prev.next \neq x` **do**
 - 3 `prev = prev.next;`
 - 4 `prev.next = x.next;`
-

Doubly Linked Lists

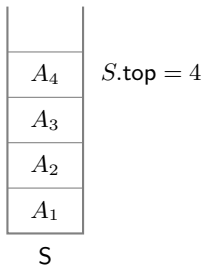


use sentinel: referring *L.nil* as *nil* yields circular, doubly linked list



Stacks

- ▷ **LIFO**: last-in, first-out
- ▷ $S.top$ = number of items in S
- ▷ operations: **push** and **pop**
- ▷ implemented by arrays (or linked-lists)



Methods

STACK-EMPTY(S)

- 1 **if** $S.top == 0$ **then return** true;
 - 2 **else return** false;
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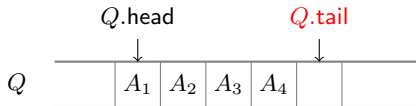
STACK-PUSH(S, x)

- 1 $S.top = S.top + 1$;
 - 2 $S[S.top] = x$;
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STACK-POP(S)

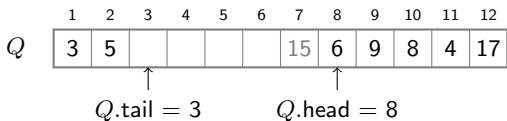
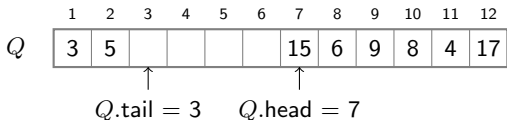
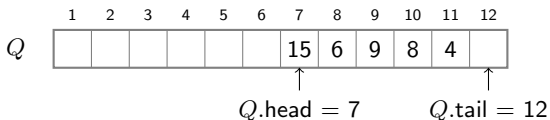
- 1 **if** STACK-EMPTY(S) **then**
 - 2 **error** "underflow";
 - 3 **else**
 - 4 $S.top = S.top - 1$;
 - 5 **return** $S[S.top + 1]$;
-

Queues



- ▷ **FIFO**: first in, first out
- ▷ $Q.head$, $Q.tail$ are keys
- ▷ operations: **enqueue** and **dequeue**
- ▷ implemented by arrays (or linked lists)

Example



note: Q has at most $n - 1$ items (for array size n) why?

Methods

ENQUEUE(Q, x)

```
1  $Q[Q.tail] = x$ ;  
2 if  $Q.tail == Q.length$  then  
3    $Q.tail = 1$ ;  
4 else  
5    $Q.tail = Q.tail + 1$ ;
```

DEQUEUE(Q)

```
1  $x = Q[Q.head]$ ;  
2 if  $Q.head == Q.length$  then  
3    $Q.head = 1$ ;  
4 else  
5    $Q.head = Q.head + 1$ ;  
6 return  $x$ ;
```
